

Widespread seismicity excitation throughout central Japan following the 2011 M=9.0 Tohoku earthquake, and its interpretation by Coulomb stress transfer

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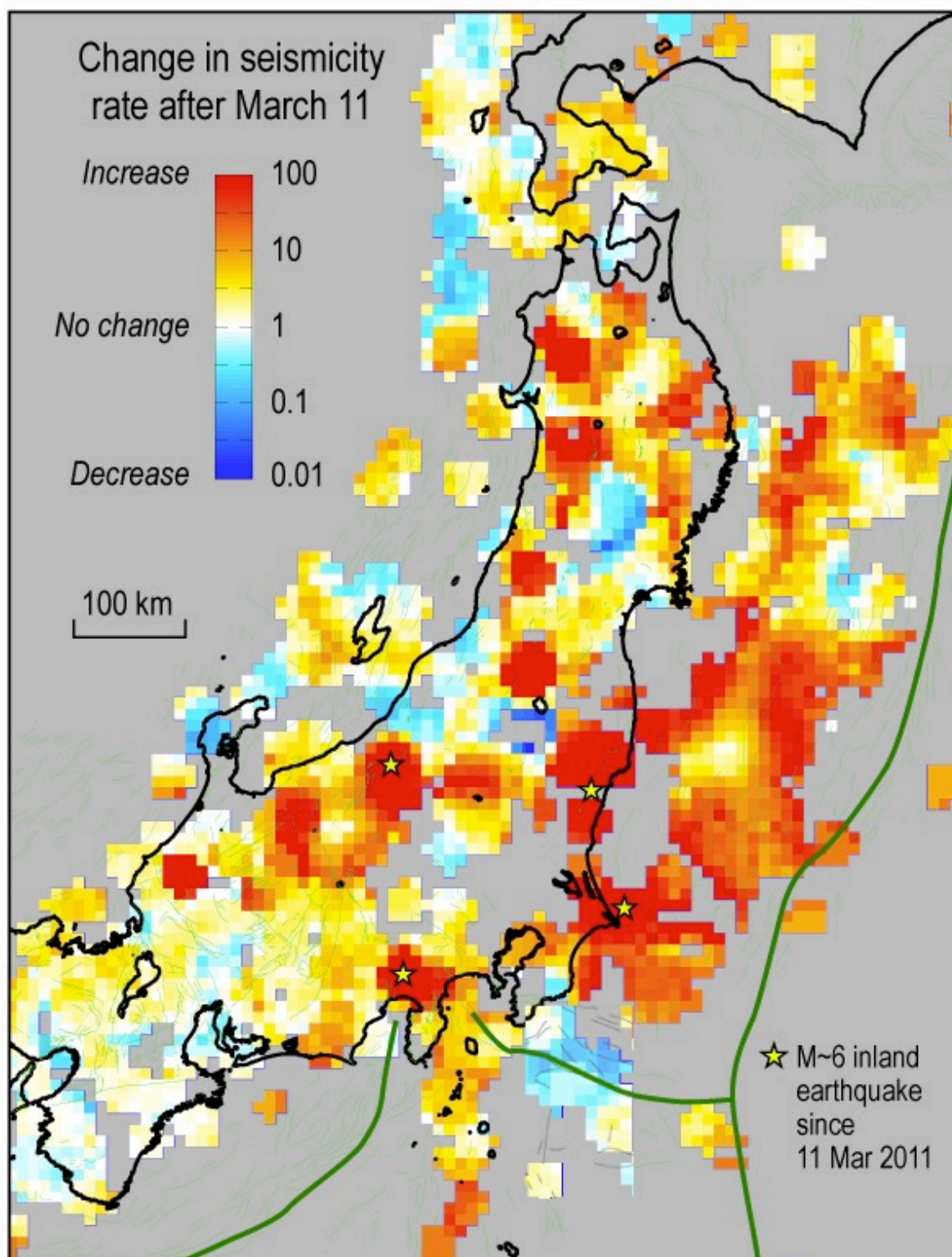
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Plain English Summary

We report on a broad and unprecedented increase in seismicity rate for microearthquakes ($M \geq 2$) over a broad 600 by 200 km (360 by 120 mi) area across inland Japan, parts of the Japan Sea and the Izu islands, following the M=9.0 Tohoku mainshock. The seismicity increase occurs at distances of up to 425 km (360 mi) from the region of high (≥ 15 m or 50 ft) seismic slip on the megathrust rupture surface of the M=9 earthquake. Are these aftershocks, and if so what do they signify for the likelihood of large earthquakes across this region? While the origin and implications of the seismicity increase is subject to debate, its occurrence is beyond dispute. It was not seen for the 2004 M=9.1 Sumatra and 2010 M=8.8 Chile earthquakes, but they lacked the seismic networks necessary to detect such small events. Here we explore the possibility that the rate changes are the product of static or permanent stress transfer from the mainshock to small surrounding faults. We find that half of the areas we can examine show a positive association between calculated stress changes and the observed seismicity rate change, three show a negative association, and in four show changes too small to assess. Regardless of the process that promotes the aftershocks, we argue that the microseismicity increases demonstrate that the ‘remote’ inland Japan and Japan Sea and shocks (e.g., the Nagano Mw=6.3 on 3/12 03:59, the Japan Sea Mw=6.2 on 3/12 04:46, the Mt. Fuji Mw=5.8 on 3/15, 22:31) are not exceptional; in fact they are not truly isolated events. Instead, they simply represent the largest shocks in a very broad zone of elevated seismicity rate that is evident for $M \geq 2$ earthquakes.



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We report on a broad and unprecedented increase in seismicity rate following the M=9.0 Tohoku mainshock for $M \geq 2$ earthquakes over inland Japan, parts of the Japan Sea and Izu islands, at distances of up to 425 km from the locus of high (≥ 15 m) seismic slip on the megathrust. Such an increase was not seen for the 2004 M=9.1 Sumatra and 2010 M=8.8 Chile earthquakes, but they lacked the seismic networks necessary to detect such small events. Here we explore the possibility that the rate changes are the product of static Coulomb stress transfer to small faults. We use the nodal planes of $M \geq 3.5$ earthquakes as proxies for such small active faults, and find that of fourteen regions averaging ~ 80 by 80 km in size, half show a positive association between calculated stress changes and the observed seismicity rate change, three show a negative correlation, and four show changes too small to assess. This work demonstrates that seismicity can turn on in the nominal stress shadow of a mainshock as long as small geometrically diverse active faults exist there, which is likely quite common.

24

25 1. Introduction

26 The M=9.0 Tohoku-chiho Taiheiyo (hereafter, 'Tohoku') earthquake resulted from slip
27 on a roughly 500-km-long and 200-km-wide seismic megathrust source (e.g., *Wei et al.*,
28 2011). Many offshore aftershocks, including four $M \geq 7$ and ~ 70 $M \geq 6$ shocks, have struck
29 during the ensuing three weeks. The possibility of other large earthquakes on adjacent
30 portions of the megathrust, similar to the 28 March 2005 Mw=8.6 Simeulue-Nias earthquake
31 following the 26 December 2004 Mw=9.1 Sumatra-Andaman earthquake [*Nalbant et al.*,
32 2005; *Pollitz et al.*, 2006] are thus possible. Sites of potential tsunamigenic earthquakes
33 include the Sanriku-Hokubu area to the north, and Off-Boso (east of the Boso peninsula) to
34 the south (Headquarters for Earthquake Research Promotion, 2005) of the 2010 Tohoku
35 rupture.

36 Equally important for the exposed population and infrastructure would be the occurrence
37 of large inland shocks in northern Honshu. Three M~6 shallow inland earthquakes have
38 already struck as far as ~ 300 km from the M=9 source within five days of the Tohoku
39 mainshock, reaffirming the broad reach and triggering potential of the great quake. Among
40 such inland sites, none is more important than Tokyo, which was last struck by the 1923
41 Kanto M=7.9 Sagami megathrust event [*Nyst et al.*, 2006], and a deeper inland event in the
42 1855 M~7.2 Ansei-Edo earthquake [*Grunewald and Stein*, 2006]. This concern is heightened
43 by several inland large earthquakes in Tohoku that have followed M=7-8 interplate events by
44 months to a decade [*Shimazaki*, 1978; *Seno*, 1979; *Churei*, 2002], including the 31 August
45 1896 Mj=7.2 Rikuu earthquake, which produced a 30-km-long surface rupture that devastated
46 the eastern Akita Prefecture (with 200 deaths).

47 To evaluate the potential triggering impact of the Tohoku earthquake to inland Japan, we
48 analyze the seismicity rate change since the Tohoku mainshock, and calculate the associated
49 static Coulomb stress changes over the region of seismicity rate change.

50

2. Inland Seismicity Rate Changes Associated with the Tohoku Earthquake

The widespread seismicity rate increase across central Japan and extending west to the Japan Sea and south to the Izu islands is evident in Figure 1. Broadly, there are strong increases in seismicity rate across a region extending up to 300 km from the distal edges of the M=9 rupture surface, and 425 km from the locus of high (≥ 15 m) seismic slip. In addition to the microseismicity, an Mj=6.7 earthquake occurred 13 hours after the Tohoku mainshock in box J, a Mj=6.4 earthquake occurred 24 hours after the Tohoku earthquake in box A, and a Mj=6.4 earthquake struck about 4.5 days after the Tohoku earthquake at the base of Mt. Fuji. While it might appear that these remote earthquakes are distinct from aftershocks closer to the rupture plane, Figure 1 suggests that it is more likely that they are simply the largest events to occur within the broad zone of increased seismicity rate.

The broad seismic excitation for Tohoku is unprecedented, although for the roughly-equivalent 2004 M=9.1 Sumatra, Indonesia, and 2010 M=8.8 Maule, Chile, earthquakes, no M<4.7 aftershock could be detected. Also, remote earthquake triggering was observed at even great distances but much lower densities following the 1992 M=7.3 Landers and 2002 M=7.9 Denali, earthquakes [Hill, 2008].

Sudden increases of post-Tohoku seismicity are observed in regions B (Akita), E (southern Fukushima – northern Ibaraki), F (Cape Inubou), H (Mt. Hotaka-Mt. Asahi), I (Kanto), where a burst of seismicity began at the head of Tokyo Bay several days after the Tohoku shock, M (Izu and islands), and K (Hida mountain range) (Figure 1). A possible increase in seismicity rate delayed by 1-3 days is observed in the box D. The increase in seismicity in regions J and A could be masked by aftershocks of the M~6 mainshocks, or the larger events could be part of the same process. The JMA (Japan Meteorological Agency) PDE catalog normally lists earthquakes that have occurred until two days before present, but because of the enormous number of aftershocks since March 11, human inspection of the records is incomplete (time series in Figure 1). Even during the first week after March 11,

data transfer interruptions caused by seismic station power outages and damage affect the earthquake record, and thus apparent seismicity rate drops might be artifacts. In contrast, sudden seismicity rate jumps are likely real. Some of the rate increases, such as boxes J and M, exhibit gradual declines since March 11 reminiscent of aftershock sequences.

3. Calculation of the Coulomb Stress Change

The static Coulomb stress change caused by a mainshock has been widely applied to assess areas of subsequent off-fault aftershocks (e.g., *Reasenbergs and Simpson, 1992*). The Coulomb stress change is defined as $\Delta CFF = \Delta\tau + \mu\Delta\sigma$, where τ is the shear stress on the fault (positive in the inferred direction of slip), σ is the normal stress (positive for fault unclamping), and μ is the apparent friction coefficient. Failure is promoted if ΔCFF is positive and inhibited if negative; both increased shear and unclamping of faults are taken to promote failure, with the influence of unclamping controlled by fault friction.

To resolve the Coulomb stress change on a ‘receiver fault’ (fault receiving stress from a mainshock) requires a source model of the earthquake fault slip, as well as the geometry and slip direction on the receiver. One can assume that the receiver faults share the same strike, dip and rake as the mainshock source fault, one can resolve stress on a major fault of known geometry (e.g., *McCloskey et al., 2003*), or one can find the receiver faults at every point that maximize the Coulomb stress increase given the earthquake stress change and the tectonic stress [*King et al., 1994*], termed the ‘optimally-oriented’ Coulomb stress change. However, the M=9.0 Tohoku earthquake at least temporarily raised the seismicity rate across a region so large that various types of faults and tectonic stress fields associated with the complex convergence of three tectonic plates are intermingled. One solution is to resolve the stress change on major active faults [*Toda et al., 2011, submitted*] based on their inferred geometry and slip sense. While this is instructive as a guide to the likelihood that one of these major faults could rupture, the faulting mechanisms of small to moderate shocks that dominate the

local seismicity increase are undoubtedly more complex and varied than the associated major structures, and so here we propose an alternative.

4. Use of Focal Mechanisms as Proxies for Small Active Faults

We instead resolve the Coulomb stress changes on the nodal planes of the abundant small earthquakes as proxies for active faults. We make use of fault plane solutions of the full, 14-year-long F-net catalog [NIED, 2011], which for inland Japan principally includes shallow crustal earthquakes of $M_j \geq 3.5$; this corresponds to source dimension ≥ 400 m [Wells and Coppersmith, 1994]. As evident by comparing the mapped active faults (green lines) with the focal mechanisms in Figures 2a and 3a, even though the mapped faults [Research Group for Active Faults in Japan, 1991] often have sinuous and en echelon traces, the focal mechanisms reveal even more complexity, such as strike-slip faults amid the mapped thrust faults of Tohoku, or thrust mechanisms with a wide range of strikes at the site of the 2008 $M_j=7.2$ Iwate-Miyagi Nairiku earthquake (box C in Figure 2a).

In Toda *et al.* [2011, submitted] we tested six representative source models and three friction values to determine the model producing the greatest gain in aftershock mechanisms promoted by the mainshock relative to the background (pre-Tohoku) mechanisms. The Wei *et al.* [2011] source model and a friction of 0.4 produces the greatest (62%) gain, and so we use them here to calculate the stress changes in an elastic half space with Poisson's ratio 0.25 and shear's modulus 3.2×10^5 bar, using Coulomb 3.2 (www.coulombstress.org). We resolve the static Coulomb stress change on both nodal planes at each hypocenter because the normal stress change is different on each plane in a set, and we do not know which of the two nodal planes slipped. In Figs. 2b and 3b, we plot the maximum Coulomb stress change for the most positive plane only (we would otherwise have to plot both sets of planes), and also place positive changes (red dots) atop negative changes (blue dots) where earthquakes overlap. Thus, the figures have an intentional 'red bias,' but Table 1 uses both nodal planes and has no

bias. We examine 14 rectangular areas where the seismicity is abundant (Figure 1) and where focal mechanisms are available (Figs. 2a and 3a).

5. Comparison of Seismicity Rate Changes and Coulomb Stress Changes

Comparison of Figure 1 with Figures 2b and 3b indicates positive associations between observed seismicity rate increases and Coulomb stress increases resolved on nodal planes in seven of the 14 boxes. We find no clear changes in either seismicity rate or stress in 4 boxes, and negative correlations, contradicting our hypothesis, in 3 boxes (Table 1).

The positive correlations include boxes F and I straddling the rupture, box M located 150-225 km from the rupture surface, and box K, 250 km from the rupture edge. In box I (Kanto district), we included mechanisms as deep as 100 km because of the complex plate configuration beneath Tokyo [Toda *et al.*, 2008]. More than 80% of the stress changes for mid to deeper shocks along the NS-trending ‘Kanto seismic corridor’ (box I) are positive.

There is also a correlation between the (albeit preliminary) seismicity rate decreases and stress decreases in boxes C, G and L. Detecting seismicity rate decreases normally demands not only a high rate of preceding seismicity, but also a long post-mainshock catalog that is not yet available. Box C was the site of the 2008 Mj=7.2 Iwate-Miyagi Nairiku earthquake, and box L was the site of the 2007 Mj=6.8 Noto Hanto earthquake; to be certain that these sites sustained seismicity rate drops, one would need to remove the expected decaying aftershock frequency from the time series. Nevertheless, the rate of aftershock decay 3-4 years after the mainshocks is low, and the observation period in Figure 1 is only one month, and so the time series in Figure 1 for at least box L appears convincing as long as post-Tohoku earthquakes are not missing from the catalog.

Inconsistent with the static stress hypothesis, box D shows a delayed rate increase but no stress increase, and there are seismicity rate increases in box A for which Coulomb stress increases are present but do not dominate. Box B lacks sufficient focal mechanisms for

confident assessment. Box J, chosen to be centered on the $M_j=6.7$ shock, shows a rate increase but a stress decrease. (Boxes N, O and P show little or no seismicity rate change or stress change; they lie up to 600 km from the Tohoku rupture.) Box E is not analyzed because the post-Tohoku seismicity is associated with shallow normal faulting, whereas the focal data contain only deep reverse mechanisms.

A majority of the mechanisms along the Ou backbone mountain range (boxes B, C and D in Figure 2b) are thought to be north-striking thrust faults, which would lie in the principal stress shadow of the Tohoku mainshock, and thus be brought farther from failure [Toda *et al.*, 2011, submitted]. However, the significant percentage of strike-slip mechanisms and thrusts of divergent strikes result in a large number of positive stress changes. This underscores that resolving stress on the major faults alone idealizes the much more complex stress transfer.

6. Discussion and Conclusions

The fundamental observation driving this study is the widespread seismicity rate increase across inland Japan, and extending to the Japan Sea and to the Izu island chain. Remarkably, seismicity turned on at distances of up to 300 km from the lower edge of the Tohoku earthquake rupture surface, and up to 425 km from the high (<15 m) slip zone. These seismicity rate increases are apparent for $M \geq 2$ earthquakes, about half the boxes include $M \geq 4$ earthquakes and in four cases include $M=5-6$ earthquakes. Most of these increases follow the Tohoku mainshock immediately, but some were delayed by up to several days. These distant aftershocks could be triggered dynamically, they could be caused by the static stress changes, or both. The maximum triggering distance, less than two source dimensions from the mainshock, is consistent with the global absence $M \geq 5$ shocks triggered at greater distances [Parsons and Velasco, 2011]. Here we explored the static hypothesis, which we adapted to the special circumstances of triggering on very small faults that are neither optimally oriented in the regional stress field nor parallel to the major faults. We thus use the Coulomb stress

change resolved on the nodal planes of the smallest earthquakes with focal mechanisms, which limits us to $M \geq 3.5$ shocks, a ≥ 400 m rupture scale that at least overlaps that of the aftershocks.

A tentative examination of the observed seismicity rate changes and calculated Coulomb stress changes has met with promising but certainly incomplete success, since we find seven positive three negative correlations (Table 1). Three of the positive correlations derive from decreases both in observed seismicity rate and calculated Coulomb stress, and while we are confident in the calculated stress decreases, it is perhaps too soon to be confident in the seismicity rate declines.

Regardless of the process that promotes the aftershocks, we argue that the microseismicity increases demonstrate that the ‘remote’ Japan Sea and inland Japan shocks (e.g., $M_w=6.3$ on 3/12 03:59, $M_w=6.2$ on 3/12 04:46, $M_w=5.8$ on 3/15, 22:31) are neither exceptional nor truly isolated events. Instead, they simply represent the largest shocks in a very broad zone of elevated seismicity rate that is evident for $M \geq 2$ earthquakes.

One of the surprises of this work is that the effect of the stress shadow expected in Tohoku for north-striking thrust fault appears—as yet—largely absent. Instead, much but not all of Tohoku exhibits an increased rate of seismicity. Here we find that this behavior is nevertheless consistent with static Coulomb stress transfer, but to smaller faults with geometries different from the major faults, a possibility first advanced by *Marsan* [2006]. One important question is whether the activation of these smaller divergent faults could trigger a large event on one of the major thrusts, as might have occurred when the 15 June 1986 $M \sim 8\frac{1}{4}$ offshore Sanriku earthquake was succeeded by the 31 August 1896 $M_j=7.2$ Rikuu inland earthquake at the same latitude (box B, Figure 2a). Since the 2011 Tohoku mainshock is about ten times larger than the Meiji Sanriku mainshock, there could be large changes in intraplate seismicity during the months to years ahead.

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Table 1

Box Fig. 1	Min. Lon. (°)	Max. Lon. (°)	Min. Lat. (°)	Max. Lat. (°)	% positive Δ CFF *	Ave. Δ CFF (bar)	Seismicity Rate Change	Correlation between rate change and Δ CFF
A	138.80	139.40	40.10	40.70	27	-0.22	Increase	Negative
C	140.50	141.00	38.70	39.30	11	-3.3	Decrease	Positive
D	139.50	140.10	37.40	38.00	14	-1.3	Delayed increase	Negative
F	140.50	141.70	35.00	36.00	75	2.5	Increase	Positive
G	139.90	141.00	33.50	35.00	37	-0.04	Decrease	Positive
H	139.20	140.00	36.50	37.30	47	0.1	Increase	—
I	139.61	140.33	35.48	36.37	83	1.2	Increase	Positive
J	138.00	139.00	36.50	37.20	15	-0.4	Increase	Negative
K	137.20	137.80	35.95	36.80	88	0.3	Increase	Positive
L	136.20	137.00	37.00	37.50	19	-0.11	Decrease	Positive
M	138.80	139.50	34.00	35.70	82	0.1	Increase	Positive
N	138.90	139.70	41.20	43.00	59	0.05	No change	—
O	135.00	136.00	34.70	35.50	17	-0.04	No change	—
P	134.75	135.50	33.75	34.35	47	0	No change	—

* Δ CFF positive > 50% (red): <50% (blue). Ave. Δ CFF value > 0 (red); <0 (blue)

The percentage of nodal planes (two for each earthquake) with Coulomb stress increases and average stress change are compared with the observed seismicity rate change. Because of the preliminary state of the aftershock catalog, the correlations are approximate.

Figure Captions

Figure 1. (Left) Seismic response of inland Japan to the $M=9.0$ Tohoku mainshock. Map of the $M \geq 1.0$ seismicity rate change (27 day post-mainshock / 1.2 year pre-mainshock), with a smoothing radius of 20 km, using the JMA PDE catalog downloaded on 9 April 2011. Except for Box G (0-100 km), all boxes use 0-20 km depth. Dark green lines show plate boundaries. (Right) Time series show cumulative numbers of $M_j \geq 0.0$ earthquakes during 1/1–3/31/2011 (blue); each earthquake is shown as a green stem proportional to magnitude, M . The catalog is likely complete for $M \geq 2.0$.

Figure 2. Coulomb stress changes resolved on the nodal planes of small earthquakes as proxies for small active faults. (a) Focal mechanisms from the F-net catalog [NIED, 2011] since 1997 (depth ≤ 20 km for inland areas, ≤ 50 km for the eastern margin of Japan Sea region, and ≤ 100 km for Kanto); D is depth. (b) Maximum Coulomb stress change from each pair of nodal planes; where earthquakes overlap, the most positively-stressed shocks are plotted atop. The color of the box boundaries indicates the overall seismicity change inside each box: Increase (red), delayed increase (red dashed), decrease (blue), and no change (black).

Figure 3. Coulomb stress changes resolved on the nodal planes of the background earthquakes as proxies of local or regional fault structure in Chubu and Kinki districts. (a) Fault plane solutions since 1997 (depth ≤ 20 km). (b) Maximum Coulomb stress change from each pair of nodal planes.

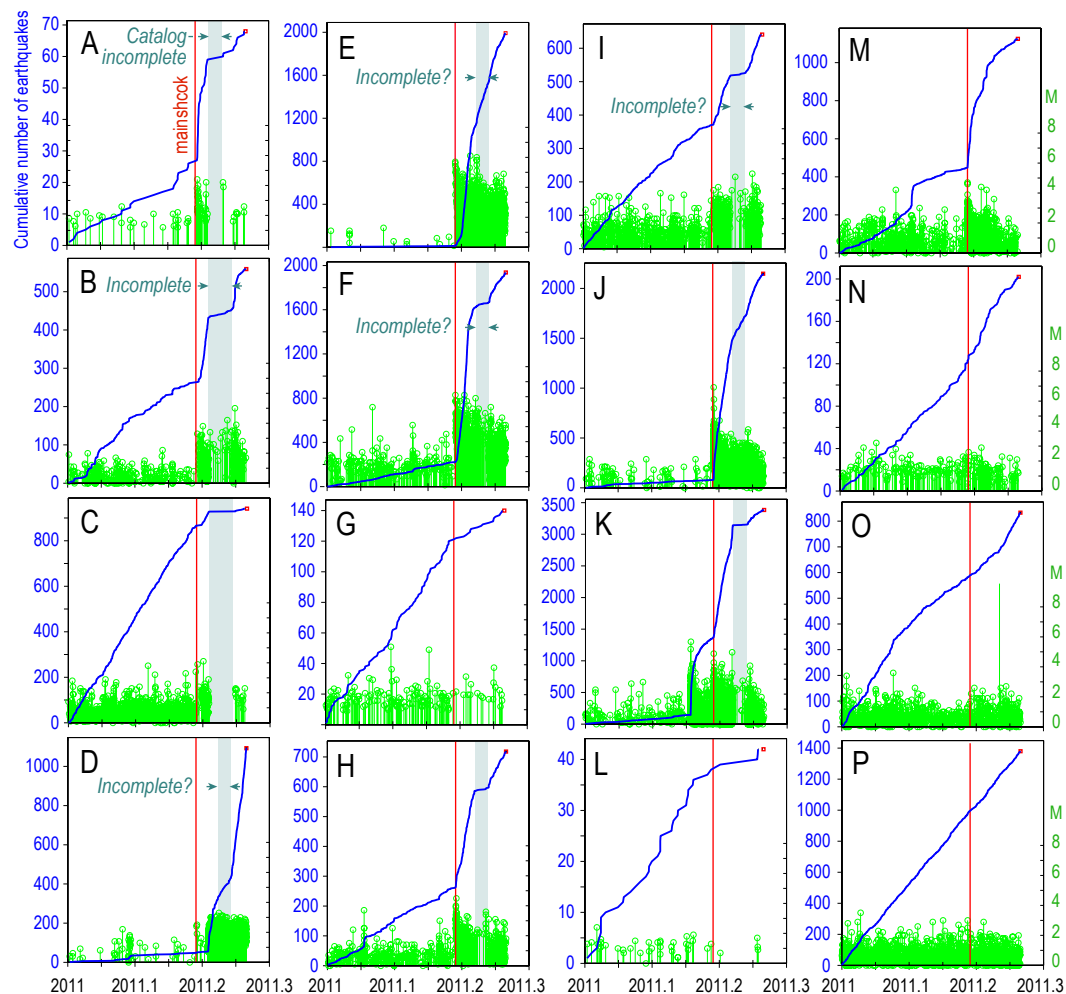
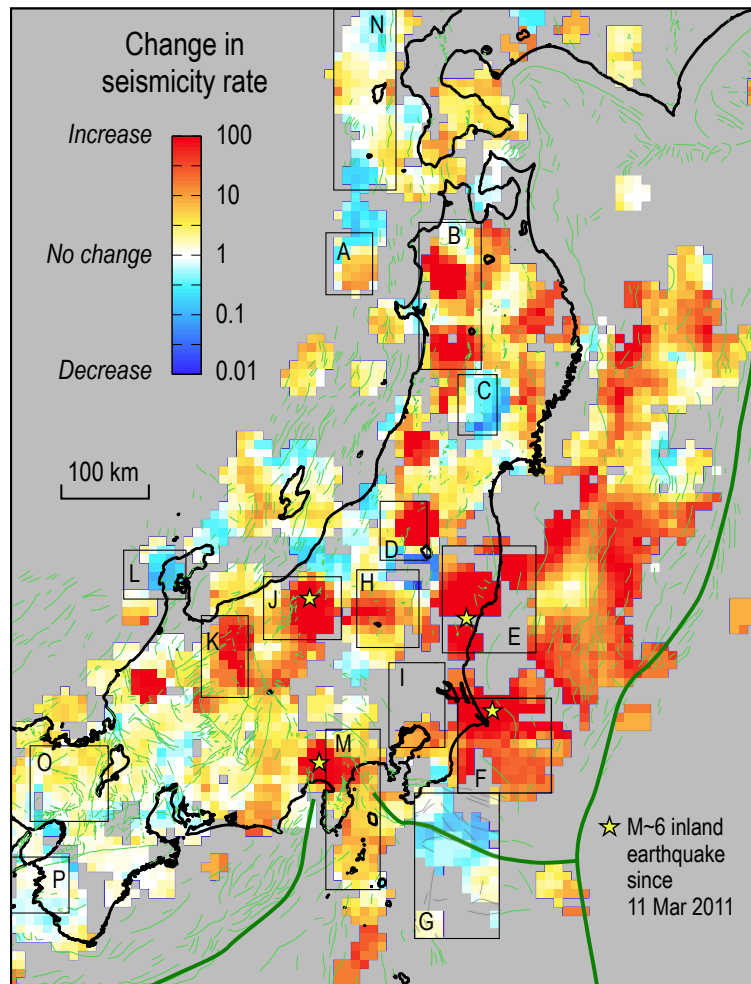


Fig. 1

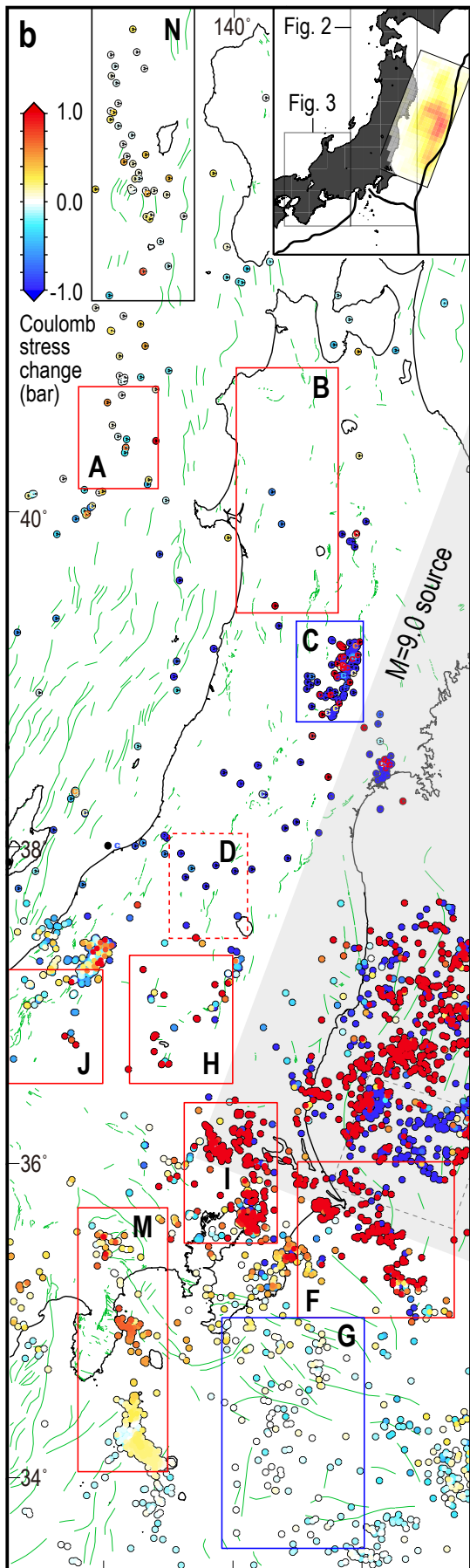
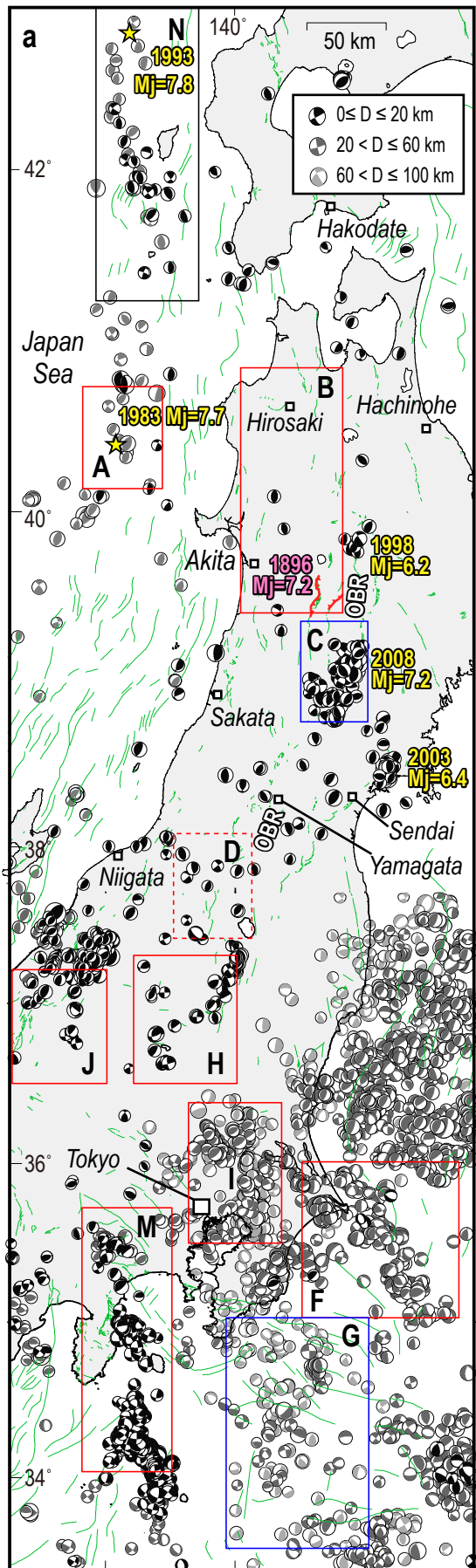


Fig. 2

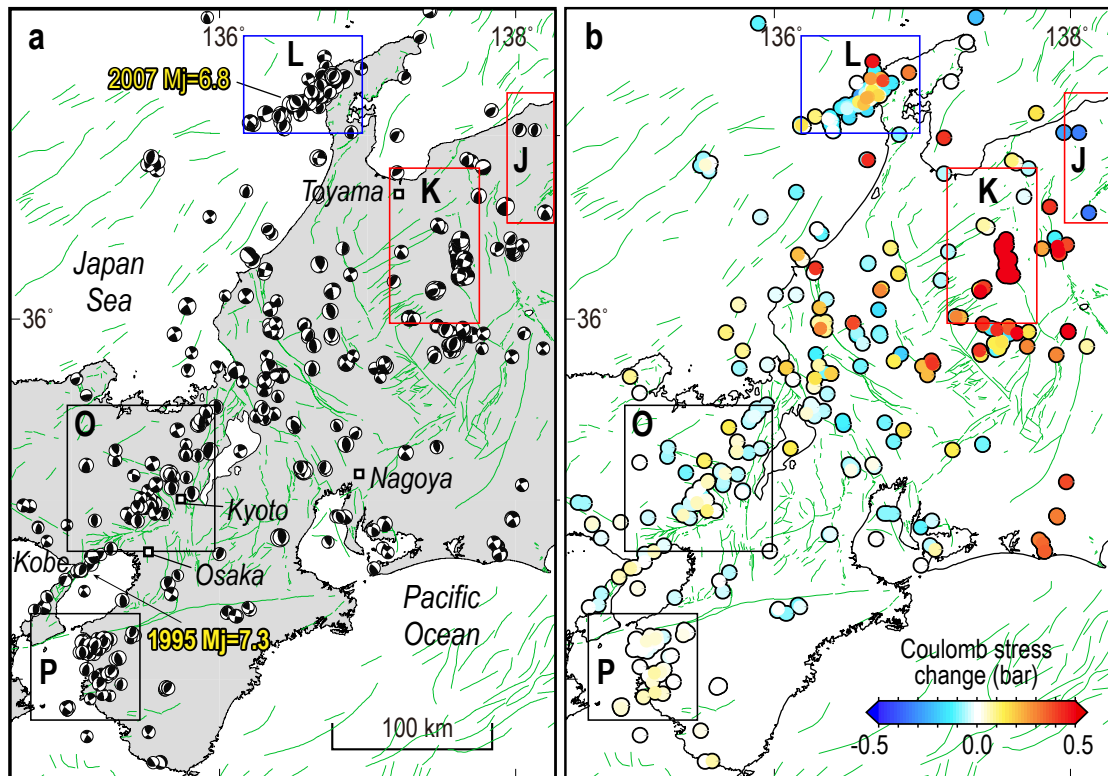


Fig. 3